## Math 206, Fall 2024 — Homework 3

## Tim Chumley

## Due September 27 at 5:00 pm

**Instructions.** This problem set contains problems from Week 3 of class. The problem numbers refer to our textbook, *Reading, Writing, and Proving* by Ulrich Daepp and Pam Gorkin.

**Problem 1.** Do the following textbook problems: Problems 5.10 (cite your work in Problem 3 below), 5.13 (remember what the range of the sine function is), 6.2, 6.5, 6.12

**Problem 2.** Write up a full proof of the triangle inequality using your work from Problem 1 of the Day 6 worksheet.

**Problem 3.** It is a standard fact that an integer n is not divisible by 3 if and only if it can be written in the form n = 3k + 1 or n = 3k + 2 for some integer k. Use this fact to prove that if  $n^2$  is divisible by 3, then n is divisible by 3.

**Problem 4.** Prove that if  $|x - 2| \le 1$  then  $|x^4 - 16| \le 65$ .