

## Math 301 — Limit points, isolated points, closed sets

**Problem 1.** Consider the set  $\{1\}$ . What are its limit points? Is it a closed set? Does it have isolated points?

**Problem 2.** Consider the set  $A = \{1/n : n \in \mathbb{N}\}$ . Explain why 0 is a limit point of  $A$ . Is  $A$  a closed set? Explain why every element of  $A$  is an isolated point.

**Problem 3.** Consider the set  $\mathbb{Q}$ . Explain why  $\mathbb{Q}$  has no isolated points and explain why  $\mathbb{R}$  is its set of limit points. Is  $\mathbb{Q}$  a closed set?

**Problem 4.** Is  $\emptyset$  a closed set? Why or why not?